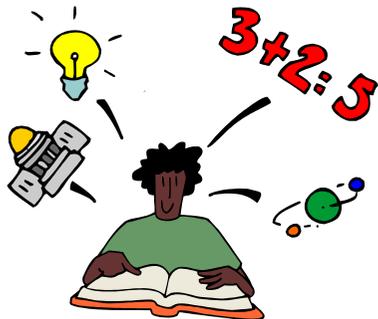


# Written Calculation Progression

## Key Stages 1 - 2



**Darell School**



Created: September 2015

# Darell School

## Pencil and paper procedures

### Background to the progression

This progression contains the key pencil and paper procedures that will be taught within our school. It has been written to ensure consistency and progression throughout the school and reflects a whole school agreement.

**Although the focus of the progression is on pencil and paper procedures, it is important to recognise that the ability to calculate mentally and to recall apply knowledge rapidly and accurately is a crucial element of the new mathematics curriculum. The mental methods in the 2014 *National Curriculum for Mathematics* will be taught systematically from Reception onwards and pupils will be given regular opportunities to develop the necessary skills; for example, through the “Maths Mountain” Strategy and through the use of *Numicon* in the Foundation Stage and Years 1 and 2. Mental calculation, however, is not at the exclusion of written recording and should be seen as complementary to and not as separate from it. In every written method, there is an element of mental processing. Sharing written methods with the teacher encourages children to think about the mental strategies that underpin them and to develop new ideas; therefore, written recording both helps children to clarify their thinking and supports and extends the development of more fluent and sophisticated mental strategies.**

During their time at Darell School, children will be encouraged to see mathematics as both a written and spoken language. Teachers will support and guide children through the following important stages:

- developing the use of pictures and a mixture of words and symbols to represent numerical activities;
- using standard symbols and conventions;
- use of jottings to aid a mental strategy and
- use of pencil and paper procedures.

**This progression concentrates on the introduction of standard symbols, the use of the empty number line as a jotting to aid mental calculation and on the introduction of pencil and paper procedures. It is important that children do not abandon jottings and mental methods once pencil and paper procedures are introduced. Children will, therefore, always be encouraged to look at a calculation/problem and then decide which is the best method to choose – pictures, mental calculation with or without jottings, or structured recording. Our long-term aim is for children to be able to select an efficient method of their choice (whether this be mental or written) that is appropriate for a given task. They will do this by always asking themselves:**

**‘Can I do this in my head?’**

**‘Can I do this in my head using drawings or jottings?’**

**‘Do I need to use a pencil and paper procedure?’**

It is vital that stages of calculation are not rushed through. Many adults find mathematics challenging because they were taught to use complex methods before they were ready. It is important, therefore, that we give children time to gain a real understanding of the mathematics they are using before they move on to more abstract methods of recording. This may mean that a child in Year 4 will still be using strategies shown as appropriate for Year 2; however, for some children it is only through constant practice of one method that true understanding comes. Other children may benefit from moving quickly through the stages or missing stages out all together. It is in this way that we ensure all children have the opportunity to experience an individualised curriculum.

# Addition

Year 1

Year 2

Year 3

## + = signs and missing numbers

Children need to understand the concept of equality before using the '=' sign. Calculations should be written either side of the equality sign so that the sign is not just interpreted as 'the answer'.

$$2 = 1 + 1$$

$$2 + 3 = 4 + 1$$

$$3 = 3$$

$$2 + 2 + 2 = 4 + 2$$

Missing numbers need to be placed in all possible places.

$$3 + 4 = \square \qquad \square = 3 + 4$$

$$3 + \square = 7 \qquad 7 = \square + 4$$

$$\square + 4 = 7 \qquad 7 = 3 + \square$$

$$\square + \nabla = 7 \qquad 7 = \square + \nabla$$

### Activities

Children should have access to a wide range of counting equipment, everyday objects, as well as hoops, sorting trays, number tracks and numbered number lines.

### Teacher modelling

Drawing jumps on numbered number lines and hundred squares to support understanding of the mental method

### Children

To create their own jumps using rulers, fingers, pens, bodies, etc.



## + = signs and missing numbers

Continue using a range of equations as in Year 1, but with appropriate, larger numbers.

Extend to

$$14 + 5 = 10 + \square$$

and

$$32 + \square + \square = 100 \quad 35 = 1 + \square + 5$$

## Partition into tens and ones and recombine

$$12 + 23 =$$

$$10 + 2 \quad 20 + 3$$

$$10 + 20 = 30$$

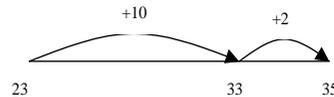
$$2 + 3 = 5$$

$$30 + 5 = 35$$

## Count on in tens and ones

Use of a numbered hundred square should be emphasised before moving on to an empty number line.

$$23 + 12 =$$



## Partitioning and bridging through 10.

The steps in addition often bridge through a multiple of 10

Children should be able to partition the 7 to relate adding the 2 and then the 5.

$$8 + 7 = 15$$

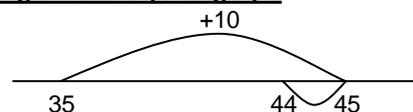


## Add 9 or 11 by adding 10 and adjusting by 1

Use of a numbered hundred square should be emphasised before moving on to an empty number line.

## Add 9 by adding 10 and adjusting by 1

$$35 + 9 = 44$$



## + = signs and missing numbers

Continue using a range of equations as in Years 1-2, but with appropriate, larger numbers.

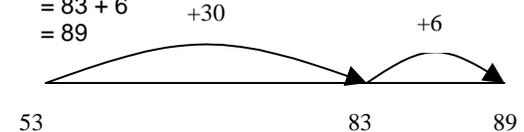
## Partition into tens and ones

- Partition both numbers and recombine.
- Count on by partitioning the second number only

$$36 + 53 = 53 + 30 + 6$$

$$= 83 + 6$$

$$= 89$$



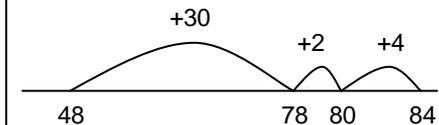
## Add a near multiple of 10 to a two-digit number

Secure mental methods by using a number line to model the method. Continue as in Year 2 but with appropriate numbers

35 + 19 is the same as 35 + 20 - 1.

Children need to be secure adding multiples of 10 to any two-digit number including those that are not multiples of 10.

$$48 + 36 = 84$$



## Pencil and paper procedures

$$83 + 42 = 125$$

## 1. Horizontal expansion then 2. Vertical expansion

$$80 + 3$$

$$+ \underline{40 + 2}$$

$$120 + 5 = 125$$

$$83$$

$$+ \underline{42}$$

$$5$$

$$\underline{120}$$

$$125$$

# Addition

## Year 4

## Year 5

## Year 6

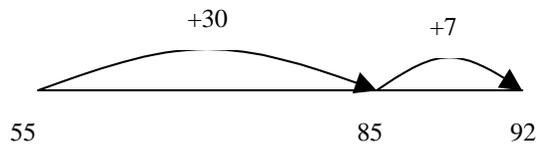
**+ = signs and missing numbers**

Continue using a range of equations as in Years 1-3, but with appropriate numbers.

**Partition into tens and ones and recombine**

Either partition both numbers and recombine or partition the second number only

$$\begin{aligned} 55 + 37 &= 55 + 30 + 7 \\ &= 85 + 7 \\ &= 92 \end{aligned}$$



**Add the nearest multiple of 10, then adjust**

Continue as in Years 2-3, but with appropriate numbers  
63 + 29 is the same as 63 + 30 - 1

**Pencil and paper procedures**

$$367 + 185 = 431$$

| First            | then    |
|------------------|---------|
| $300 + 60 + 7$   | $367$   |
| $+ 100 + 80 + 5$ | $+ 185$ |
| $400 + 140 + 12$ | $12$    |
|                  | $140$   |
|                  | $400$   |
|                  | $552$   |

**leading to**

$$\begin{array}{r} 367 \\ +185 \\ \hline 552 \\ \small{11} \end{array}$$

Recording of 'carrying' can be done at the bottom or at the top.

Extend to decimals in the context of money.

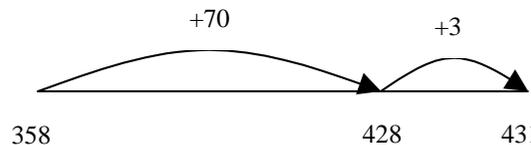
**+ = signs and missing numbers**

Continue using a range of equations as in Years 1-4, but with appropriate numbers.

**Partition into hundreds, tens and ones and recombine**

Partition the second number only and recombine

$$\begin{aligned} 358 + 73 &= 358 + 70 + 3 \\ &= 428 + 3 \\ &= 431 \end{aligned}$$



**Add or subtract the nearest multiple of 10 or 100, then adjust**

Continue as in Years 2-4, but with appropriate numbers  
458 + 79 = is the same as 458 + 80 - 1

**Pencil and paper procedures**

Extend to numbers with at least four digits  
3587 + 675 = 4262

$$\begin{array}{r} 3587 \\ + 675 \\ \hline 4262 \\ \small{111} \end{array}$$

Revert to expanded methods if the children experience any difficulty.

Adding more than two numbers together e.g. 3891 + 245 + 37

Extend to up to two places of decimals (same number of decimals places) and adding several numbers (with different numbers of digits).

$$\begin{array}{r} 72.8 \\ + 54.6 \\ \hline 127.4 \end{array}$$

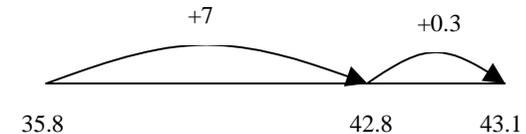
**+ = signs and missing numbers**

Continue using a range of equations as in Years 1-5, but with appropriate numbers.

**Partition into hundreds, tens, ones and decimal fractions and recombine**

Either partition both numbers and recombine or partition the second number only e.g.

$$\begin{aligned} 35.8 + 7.3 &= 35.8 + 7 + 0.3 \\ &= 42.8 + 0.3 \\ &= 43.1 \end{aligned}$$



**Add the nearest multiple of 10, 100 or 1000, then adjust**

Continue as in Years 2-5, but with appropriate numbers, including extending to adding 0.9, 1.9, 2.9, etc.

**Pencil and paper procedures**

Extend to numbers with any number of digits and decimals with 1, 2 and/or 3 decimal places.

$$13.86 + 9.481 = 23.341$$

$$\begin{array}{r} 13.860 \\ + 9.481 \\ \hline 23.341 \\ \small{111} \end{array}$$

Zero added into the thousandths column to ensure the same number of decimal places.

Revert to expanded methods if the children experience any difficulty.

Children to add more than two numbers together (with different numbers of digits and including decimal numbers) e.g. 368.4 + 98.27 + 0.08

# Subtraction

## Year 1

## Year 2

## Year 3

### - = signs and missing numbers

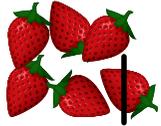
$$7 - 3 = \square \quad \square = 7 - 3$$

$$7 - \square = 4 \quad 4 = \square - 3$$

$$\square - 3 = 4 \quad 4 = 7 - \square$$

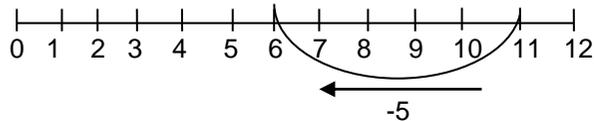
$$\square - \nabla = 4 \quad 4 = \square - \nabla$$

- Understand subtraction as 'take away'



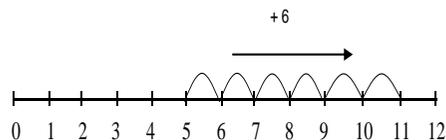
- Use practical and informal written methods to support the subtraction of a one-digit number from a one digit or two-digit number and a multiple of 10 from a two-digit number.

I have 11 toy cars. There are 5 cars too many to fit in the garage. How many cars fit in the garage?



- Find a 'difference' by counting up;

I have saved 5p. The socks that I want to buy cost 11p. How much more do I need in order to buy the socks?



Use the vocabulary related to addition and subtraction and symbols to describe and record addition and subtraction number sentences

Recording by

- drawing jumps on prepared lines and hundred squares
- constructing own lines

### - = signs and missing numbers

Continue using a range of equations as in Year 1, but with appropriate numbers.

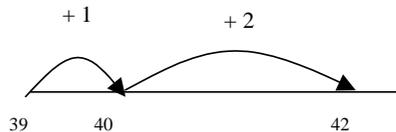
Extend to  $14 + 5 = 20 - \square$

$$\square - 5 = 13$$

### Find a small difference by counting up

Use of a numbered number line or hundred square should be emphasised before moving on to an empty number line.

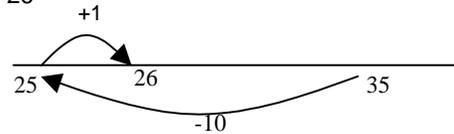
$$42 - 39 = 3$$



### Subtract 9 or 11. Begin to add/subtract 19 or 21

Use of a numbered hundred square should be emphasised before moving on to an empty number line.

$$35 - 9 = 26$$



### Use known number facts and place value to subtract

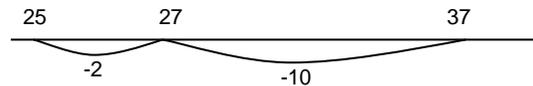
Use of a numbered hundred square should be emphasised before moving on to an empty number line.

(partition second number only)

$$37 - 12 = 37 - 10 - 2$$

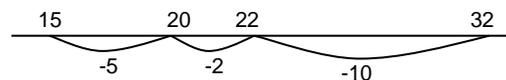
$$= 27 - 2$$

$$= 25$$



### Bridge through 10 where necessary

$$32 - 17 = 15$$



### - = signs and missing numbers

Continue using a range of equations as in Years 1-2, but with appropriate numbers

### Find a small difference by counting up

Use of a numbered number line or hundred square should be emphasised before moving on to an empty number line. Continue as in Years 1-2, but with appropriate numbers

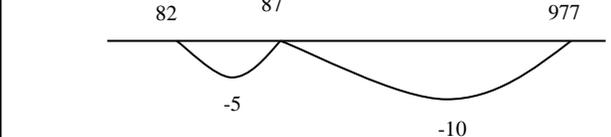
### Subtract mentally a 'near multiple of 10' from a two-digit number

Continue as in Year 2, but with appropriate numbers

### Use known number facts and place value to subtract

Use of a numbered hundred square should be emphasised before moving on to an empty number line.

Continue as in Year 2, but with appropriate numbers, e.g.

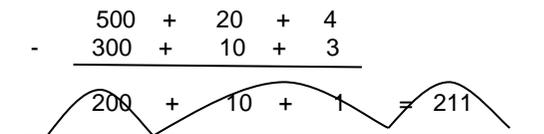


With practice, children will need to record less information and decide whether to count back or forward. It is useful to ask children whether counting up or back is the more efficient, such as  $57 - 12$ ,  $86 - 77$  or  $43 - 28$ .

### Pencil and paper procedures

Partitioning with no exchange.

$$524 - 313 = 211$$



# Subtraction

Year 4

Year 5

Year 6

**- = signs and missing numbers**

Continue using a range of equations as in Years 1-3, but with appropriate numbers.

**Find a small difference by counting up**

$5003 - 4996 = 7$

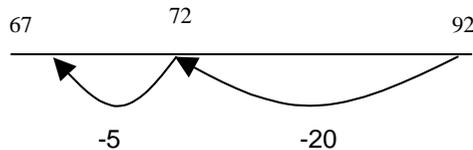
This can be modelled on an empty number line (see complementary addition below). Children should be encouraged to use known number facts to reduce the number of steps.

**Subtract the nearest multiple of 10, then adjust.**

Continue as in Years 2-3, but with appropriate numbers.

**Use known number facts and place value to subtract**

$92 - 25 = 67$



**Pencil and paper procedures**

Complementary addition

*For those children with a secure mental image of the number line they could record the jumps only:*

$754 - 86 = 668$

$$\begin{array}{r} 14 \text{ (100)} \\ 600 \text{ (700)} \\ \underline{54 \text{ (754)}} \\ 668 \end{array}$$

Partitioning with exchange

Progression of decomposition is shown in the appendix.

**- = signs and missing numbers**

Continue using a range of equations as in Years 1-4, but with appropriate numbers.

**Find a difference by counting up**

$8006 - 2993 = 5013$

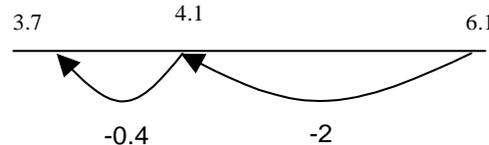
This can be modelled on an empty number line (see complementary addition below).

**Subtract the nearest multiple of 10 or 100, then adjust.**

Continue as in Year 2-4, but with appropriate numbers.

**Use known number facts and place value to subtract**

$6.1 - 2.4 = 3.7$



**Pencil and paper procedures**

Complementary addition

$754 - 286 = 468$

|                                |                   |                     |
|--------------------------------|-------------------|---------------------|
| $14 \text{ (300)}$             | can be refined to | $14 \text{ (300)}$  |
| $400 \text{ (700)}$            |                   | $454 \text{ (754)}$ |
| $\underline{54 \text{ (754)}}$ |                   | $468$               |
| $468$                          |                   |                     |

Reduce the number of steps to make the calculation more efficient.

Transition from the partitioning method used in Year 4 (see appendix) to using the compact method of decomposition, including decimals.

$78.4 - 25.6 = 42.8$

$$\begin{array}{r} 78.4 \\ - 25.6 \\ \hline 52.8 \end{array}$$

**- = signs and missing numbers**

Continue using a range of equations as in Years 1-5, but with appropriate numbers.

**Find a difference by counting up**

$8000 - 2785 = 5215$

To make this method more efficient, the number of steps should be reduced to a minimum through children knowing

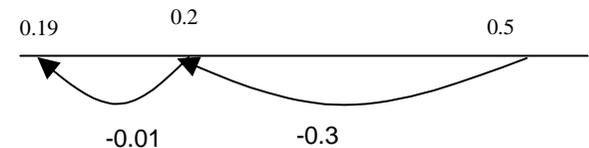
- Complements to 1, involving decimals to two decimal places (  $0.16 + 0.84$  )
- Complements to 10, 100 and 100

**Subtract the nearest multiple of 10, 100 or 1000, then adjust**

Continue as in Years 2-5, but with appropriate numbers.

**Use known number facts and place value to subtract**

$0.5 - 0.31 = 0.19$



**Pencil and paper procedures**

Complementary addition:  $6467 - 2684 = 3783$

$6467 - 2684 = 3783$

|                                   |                   |                       |
|-----------------------------------|-------------------|-----------------------|
| $16 \text{ (2700)}$               | can be refined to | $316 \text{ (3000)}$  |
| $300 \text{ (3000)}$              |                   | $3467 \text{ (6467)}$ |
| $\underline{3467 \text{ (6467)}}$ |                   | $3783$                |
| $3783$                            |                   |                       |

Reduce the number of steps to make the calculation more efficient.

Extend to 2 places of decimals and decomposition. Progression of decomposition is shown in the appendix.

# Multiplication

## Year 1

## Year 2

## Year 3

Multiplication is related to doubling and counting groups of the same size.



Looking at columns  
 $2 + 2 + 2$   
 3 groups of 2

Looking at rows  
 $3 + 3$   
 2 groups of 3

### Counting using a variety of practical resources

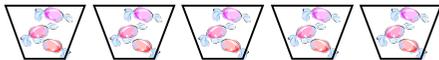
Counting in 2s, e.g., counting socks, shoes, animals' legs...

Counting in 5s, e.g., counting fingers, fingers in gloves, toes...

Counting in 10s, e.g., fingers, toes...

### **Pictures/marks**

There are 3 sweets in one bag.  
 How many sweets are there in 5 bags?



### x = signs and missing numbers

$$7 \times 2 = \square \quad \square = 2 \times 7$$

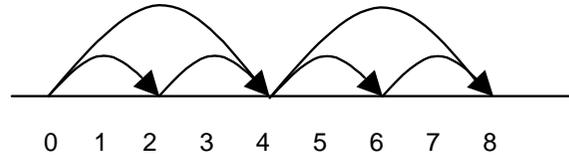
$$7 \times \square = 14 \quad 14 = \square \times 7$$

$$\square \times 2 = 14 \quad 14 = 2 \times \square$$

$$\square \times \nabla = 14 \quad 14 = \square \times \nabla$$

### Arrays and repeated addition

$4 \times 2$  or  $2 + 2 + 2 + 2$   
 $2 \times 4$  or  $4 + 4$



### Doubling multiples of 5 up to 50

$$2 \times 15 = 30$$

Partition

Children need to be secure with partitioning numbers into 10s and 1s and partitioning in different ways:  $6 = 5 + 1$  so for example, double 6 is the same as double five add double one.

$$10 + 5$$

AND double 15

$$20 + 10 = 30$$

OR

(smaller number along left side)

|   |    |    |      |
|---|----|----|------|
| x | 10 | 5  |      |
| 2 | 20 | 10 | = 30 |

### x = signs and missing numbers

Continue using a range of equations as in Year 2 but with appropriate numbers.

### Arrays and repeated addition

Continue to understand multiplication as repeated addition and continue to use arrays (as in Year 2).

### Doubling multiples of 5 up to 50

$$35 \times 2 = 70$$

Partition

(smaller number along left side)

|   |    |    |      |
|---|----|----|------|
| x | 30 | 5  |      |
| 2 | 60 | 10 | = 70 |

### Use known facts and place value to carry out simple multiplications

Use the same method as above (partitioning)

$$72 \times 38 = 2100 + 560 + 60 + 16 = 2736$$

|    |      |    |  |
|----|------|----|--|
| x  | 70   | 2  |  |
| 30 | 2100 | 60 |  |
| 8  | 560  | 16 |  |

# Multiplication

## Year 4

## Year 5

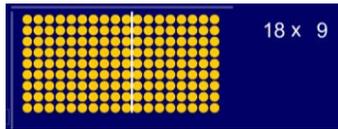
## Year 6

**x = signs and missing numbers**

Continue using a range of equations as in Years 2 and 3, but with appropriate numbers

**Partition**

Continue to use arrays:



$18 \times 9 = 162$

$18 \times 9 = (10 \times 9) + (8 \times 9) = 162$

**OR**

Use the grid method of multiplication (as below) (smaller number along left side)

**Pencil and paper procedures**

Continue use of grid method, as taught in Year 3.

Move on to using the expanded method of multiplication

$$\begin{array}{r}
 234 \times 8 \\
 \begin{array}{r}
 234 \\
 \times 8 \\
 \hline
 32 \quad (4 \times 8) \\
 240 \quad (30 \times 8) \\
 1600 \quad (200 \times 8) \\
 \hline
 1872
 \end{array}
 \end{array}$$

**x = signs and missing numbers**

Continue using a range of equations as in Years 2-4 but with appropriate numbers

**Partition**

$47 \times 6 = 282$

$47 \times 6 = (40 \times 6) + (7 \times 6) = 282$

**Pencil and paper procedures**

Use grid method to introduce multiplying decimals

$3.7 \times 4 = 14.8$

$$\begin{array}{r|l|l}
 X & 3 & 0.7 \\
 \hline
 4 & 12 & 2.8 \\
 \hline
 & & = 14.8
 \end{array}$$

Use expanded method of multiplication (see Year 4) then move on to the short method of multiplication.

$45 \times 38 =$

$$\begin{array}{r}
 \begin{array}{r}
 45 \\
 \times 38 \\
 \hline
 40 \quad (5 \times 8) \\
 320 \quad (40 \times 8) \\
 150 \quad (5 \times 30) \\
 1200 \quad (40 \times 30) \\
 \hline
 1710 \\
 \hline
 1
 \end{array}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{r}
 45 \\
 \times 38 \\
 \hline
 360 \\
 1350 \\
 \hline
 1710 \\
 \hline
 1
 \end{array}
 \end{array}$$

**x = signs and missing numbers**

Continue using a range of equations as in Years 2-5, but with appropriate numbers

**Partition**

$87 \times 6 = 522$

$87 \times 6 = (80 \times 6) + (7 \times 6) = 522$

**OR**

Use the short method of multiplication (see below)

**Pencil and paper procedures**

$$\begin{array}{r}
 231 \times 16 \\
 \begin{array}{r}
 231 \\
 \times 16 \\
 \hline
 1386 \\
 2310 \\
 \hline
 3696
 \end{array}
 \end{array}$$

Use the short method to multiply calculations involving decimals

$14.6 \times 7 =$

First remove the decimal point

$$\begin{array}{r}
 \begin{array}{r}
 146 \\
 \times 7 \\
 \hline
 1022
 \end{array}
 \end{array}$$

Then reintroduce the decimal into the answer = 102.2

# Division

Year 1

Year 2

Year 3

## Sharing

Requires secure counting skills  
-see counting and understanding number strand  
Develops importance of one-to-one correspondence

Sharing – 6 sweets are shared between 2 people. How many do they have each?



Practical activities involving sharing, distributing cards when playing a game, putting objects onto plates, into cups, hoops, etc.

## Grouping

Sorting objects into 2s/3s/4s, etc.  
How many pairs of socks are there?



There are 12 crocus bulbs. Plant 3 in each pot. How many pots are there?  
Jo has 12 Lego wheels. How many cars can she make?

## ÷ = signs and missing numbers

$$\begin{array}{ll} 6 \div 2 = \square & \square = 6 \div 2 \\ 6 \div \square = 3 & 3 = 6 \div \square \\ \square \div 2 = 3 & 3 = \square \div 2 \\ \square \div \nabla = 3 & 3 = \square \div \nabla \end{array}$$

## Grouping

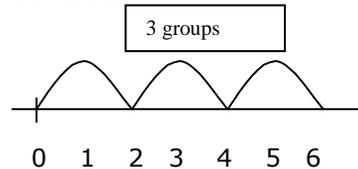
Link to counting and understanding number strand  
Count up to 100 objects by grouping them and counting in tens, fives or twos;

Find one half, one quarter and three quarters of shapes and sets of objects

$6 \div 2$  can be modelled as:

There are 6 strawberries. How many 2s in 6?  
How many people can have 2 each?

$6 \div 2$  can be modelled as:



In the context of money count forwards and backwards using 2p, 5p and 10p coins

Practical grouping, e.g., in PE

12 children get into teams of 4 to play a game. How many teams are there?



## Sharing

Continue as in Year 1, using a more formal recording method with the division symbol.

Link division facts to times tables.

## ÷ = signs and missing numbers

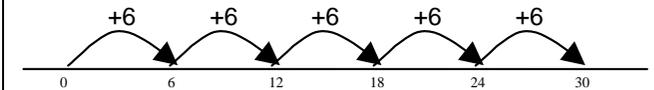
Continue using a range of equations as in Year 2 but with appropriate numbers.

## Understand division as sharing and grouping

### Sharing and grouping

$30 \div 6$  can be modelled as:

grouping – groups of 6 placed on no. line and the number of groups counted



Sharing – sharing among 6, the number given to each person

## Remainders

$$16 \div 3 = 5 \text{ r}1$$

Grouping – How many 3s in 16; how many left over?

Sharing – 16 shared between 3; how many left over?



## Pencil and paper procedures

$72 \div 5$  lies between  $50 \div 5 = 10$  and  $100 \div 5 = 20$

\* Partition the dividend into multiples of the divisor:

$$72 = 50 + 22$$

$$50 \div 5 = 10$$

$$22 \div 5 = 4 \text{ r}2 \rightarrow 10 + 4 \text{ r}2 = 14 \text{ r}2$$

$$\begin{array}{r} 72 \\ \downarrow \quad \downarrow \\ 50 + 22 \\ \downarrow \quad \downarrow \\ 10 + 4 \text{ r}2 \end{array}$$

Answer : 14 r 2

# Division

## Year 5

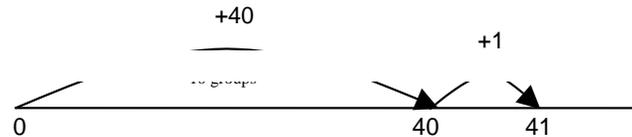
### Year 4

#### ÷ = signs and missing numbers

Continue using a range of equations as in Years 2-3, but with appropriate numbers.

#### Remainders

$$41 \div 4 = 10 \text{ r}1$$



$$41 = (10 \times 4) + 1$$

#### Pencil and paper procedures

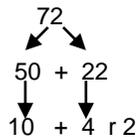
$72 \div 5$  lies between  $50 \div 5 = 10$  and  $100 \div 5 = 20$

\* Partition the dividend into multiples of the divisor:

$$72 = 50 + 22$$

$$50 \div 5 = 10$$

$$22 \div 5 = 4\text{r}2 \rightarrow 10 + 4\text{r}2 = 14\text{r}2$$



Answer : 14 r 2

Then move on to the expanded bus stop method for division

$$10 + 4 \text{ r}2 = 14 \text{ r}2$$

$$\begin{array}{r} 5 \overline{) 72} \\ - 50 \\ \hline 22 \\ - 20 \\ \hline 2 \end{array}$$

### Year 6

#### ÷ = signs and missing numbers

Continue using a range of equations as in Years 2-5, but with appropriate numbers.

#### Sharing and grouping

Continue to understand division as both sharing and grouping (repeated subtraction).

#### Remainders

Quotients expressed as fractions or decimals

$$676 \div 8 = 84 \frac{1}{2} \text{ or } 84.5$$

#### Pencil and paper procedures

$977 \div 36$  is approximately  $1000 \div 40 = 25$

#### Compact bus stop method

$$\begin{array}{r} 032 \text{ r}4 \\ 6 \overline{) 41916} \end{array}$$

$$46.8 \div 3 = 15.9$$

$$\begin{array}{r} 15.9 \\ 3 \overline{) 417.27} \end{array}$$

Continue to use long division (see Year 5)

#### ÷ = signs and missing numbers

Continue using a range of equations as in Years 2-4, but with appropriate numbers.

#### Sharing and grouping

Continue to understand division as both sharing and grouping (repeated subtraction).

#### Remainders

Quotients expressed as fractions or decimals

$$61 \div 4 = 15 \frac{1}{4} \text{ or } 15.25$$

#### Pencil and paper procedures

$196 \div 6$  lies between  $180 \div 6 = 30$  and  $240 \div 6 = 40$

#### Expanded bus stop method

$$\begin{array}{r} 30 + 2 \text{ r}4 \\ 6 \overline{) 196} \\ - 180 \\ \hline 16 \\ - 12 \\ \hline 4 \end{array} \quad \text{Answer: } 32 \text{ r}4$$

#### Long division

$$\begin{array}{r} 32 \text{ r}4 \\ 6 \overline{) 196} \\ - 18 \downarrow \\ \hline 16 \\ - 12 \\ \hline 4 \end{array}$$